

# Nanoparticle clusters:

## An introduction to small-angle x-ray scattering (SAXS)

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*Earth Sciences Division*

*Lawrence Berkeley National Lab.*



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# Collaborators

## Goethite nanoparticles:

- **Chris Kim** Chapman University, CA
  - Nanogoethite synthesis and characterization
- **Guopeng Lu** LBNL
  - Lattice Boltzmann simulation
- **Mike Toney** SSRL
  - Simulated annealing

## SSRL Scientific support:

- **John Pople**

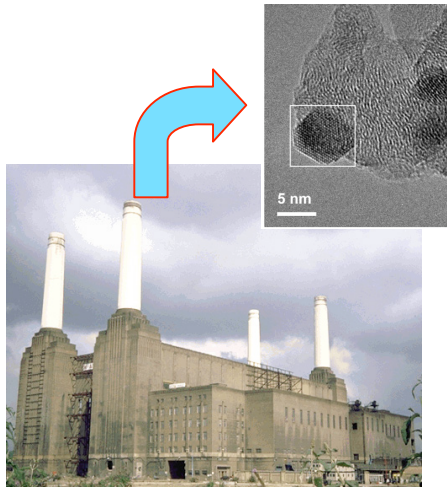
**Funding - LBNL LDRD & DOE BES**



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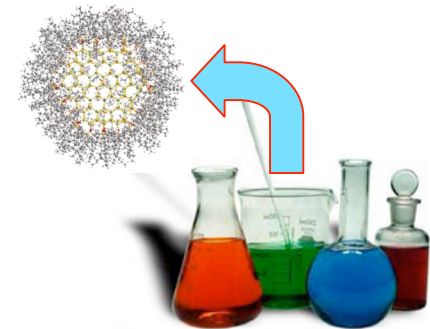
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# Sources of Nanominerals



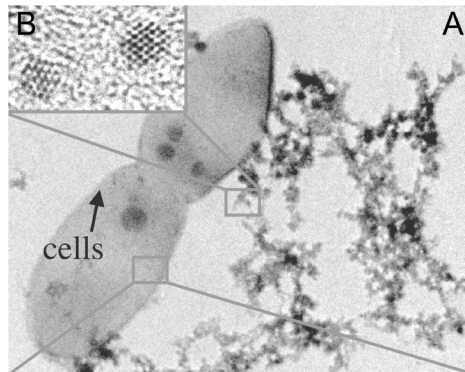
*Combustion products*

## Man-made

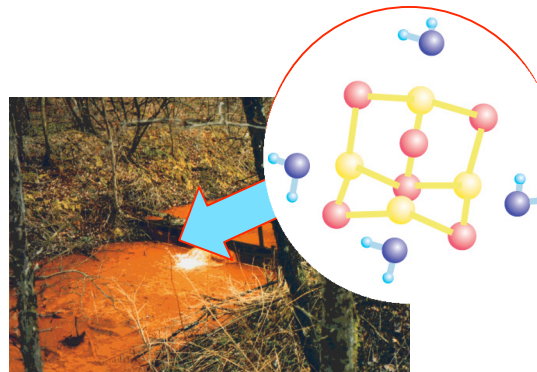


*Chemical synthesis*

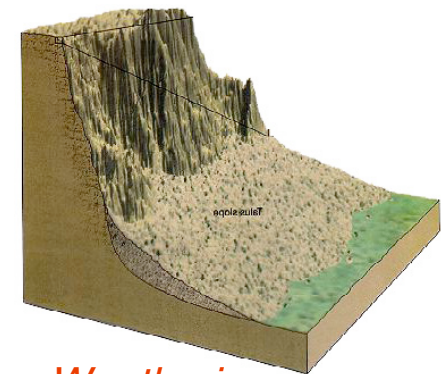
## Natural



*Biomineralization*



*Inorganic precipitation*



*Weathering*

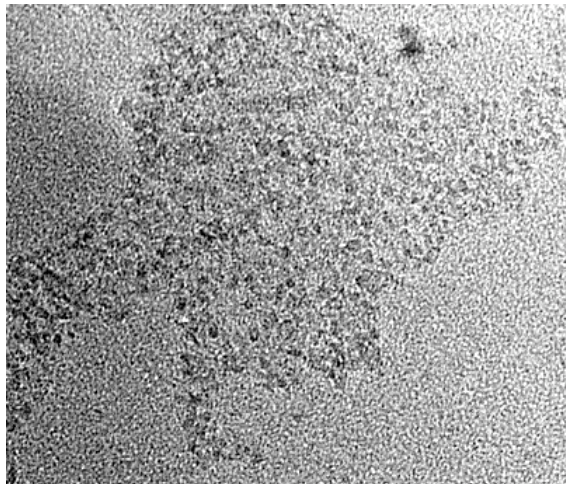


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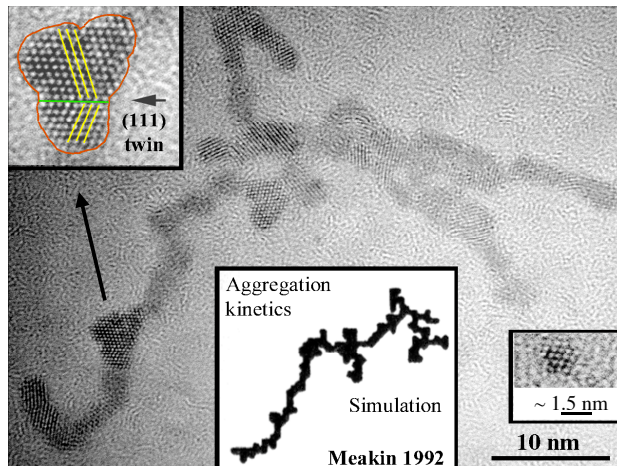
# Nanoparticle Aggregation Morphologies

*$\alpha$ -FeOOH nanoparticles*



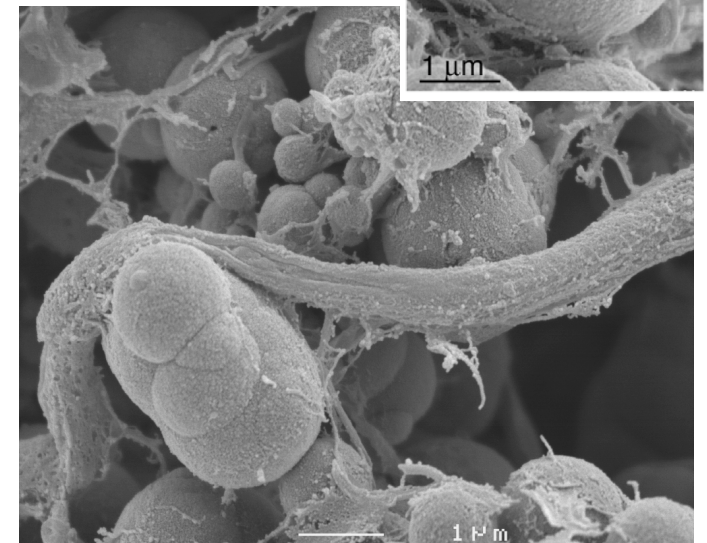
Chris Kim  
unpublished

*Biogenic UO<sub>2</sub> nanoparticles*



Suzuki et al., *Nature* **419**, 134 (2002)

*Biogenic ZnS nanoparticles*



Labrenz et al., *Science* **290**, 1744 (2000)



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# Consequences of Aggregation

- Mineral Growth
  - Aggregation-based pathways
- Transport
  - Bioremediation efficacy
- Surface Geochemical Processes
  - Ligand-mediated dissolution
- Detection
  - Induced polarization methods

# Nanoparticles in Aqueous Environments

## 1 • Under what conditions do nanoparticles aggregate?

- Size, solution chemistry *experiment*
- Derive interparticle forces *modeling*

## 2 • What aggregate structures are formed?

- Measure cluster size, morphology, density *experiment*
- Simulate aggregation processes *modeling*

## 3 • How do aggregates travel through porous media?

- Flow column experiments *experiment*
- Simulate settling and straining effects *modeling*



# Nanoparticles in Aqueous Environments

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Small-angle  
x-ray  
scattering

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# Small-angle X-ray Scattering

## Suggested reading:

**Neutron, X-ray and Light Scattering:**  
Introduction to an Investigative Tool for  
Colloidal and Polymeric Systems

P. Lindner & Th. Zemb (Eds.)

North-Holland, Amsterdam, 1991

[www.alibris.com](http://www.alibris.com)

[www.zubalbooks.com](http://www.zubalbooks.com)



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# X-ray scattering basics

$$q = \frac{4\pi}{\lambda} \sin \theta$$

$$q = \frac{2\pi}{d}$$

- SAXS: small-angle x-ray scattering

$$10^{-3} \text{ \AA}^{-1} < q_{max} < 0.1 \text{ \AA}^{-1}$$

- Scattering from electron density contrast

- WAXS: wide-angle x-ray scattering

$$0 < q_{max} < 5 \text{ \AA}^{-1}$$

- Equivalent to conventional X-ray Diffraction (XRD)

- High-energy WAXS:

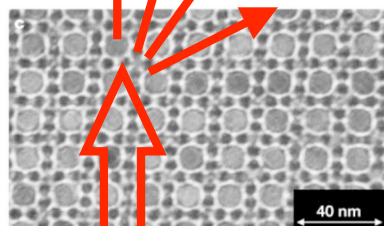
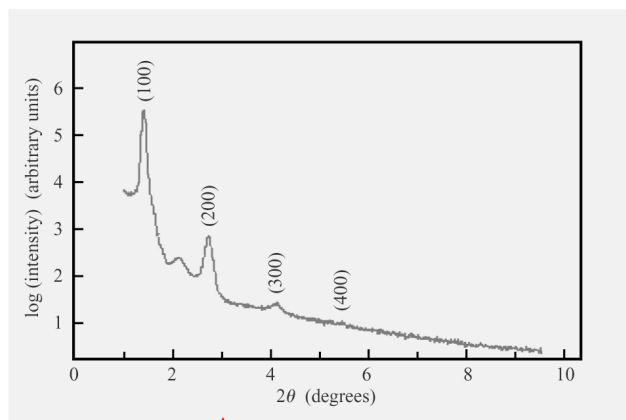
$$q_{max} > 20 \text{ \AA}^{-1}$$

- Fourier inversion provides the real-space Pair Distribution Function



# Small-angle X-ray Scattering

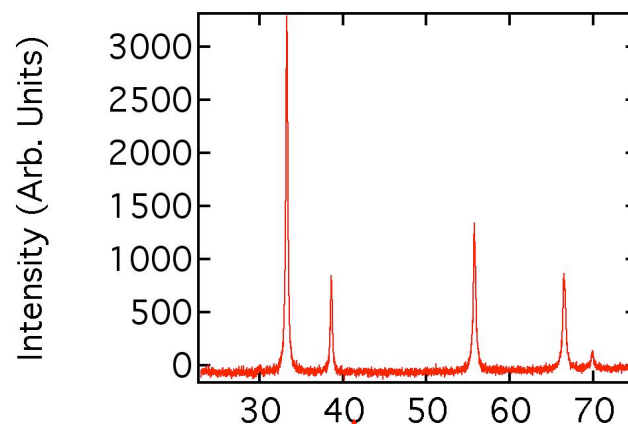
**SAXS = diffraction from particles**



oriented  $\text{Fe}_2\text{O}_3$   
and PbS  
nanoparticles

x-rays

**WAXS = XRD = diffraction from atoms**



ZnS crystal

x-rays



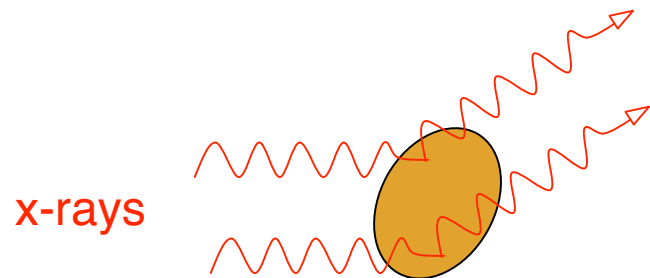
Redl et al., *Nature* **423**, 968 (2003)

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# Small-angle X-ray Scattering

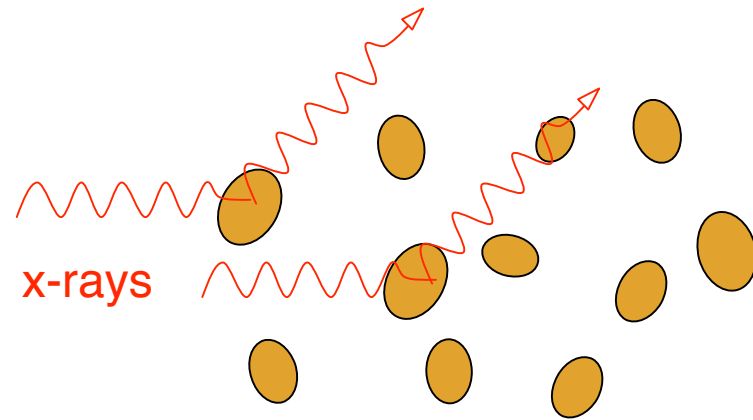
$P(q)$  = particle scattering



Dilute solutions:

$$I(q) = P(q)$$

$S(q)$  = interparticle scattering



Concentrated solutions or aggregates:

$$I(q) = S(q)P(q)$$

(identical particles)

Scattering vs.  $q$ , not  $\theta$  :

$$q = \frac{4\pi}{\lambda} \sin \theta$$

$$q = \frac{2\pi}{d}$$



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# Small-angle X-ray Scattering

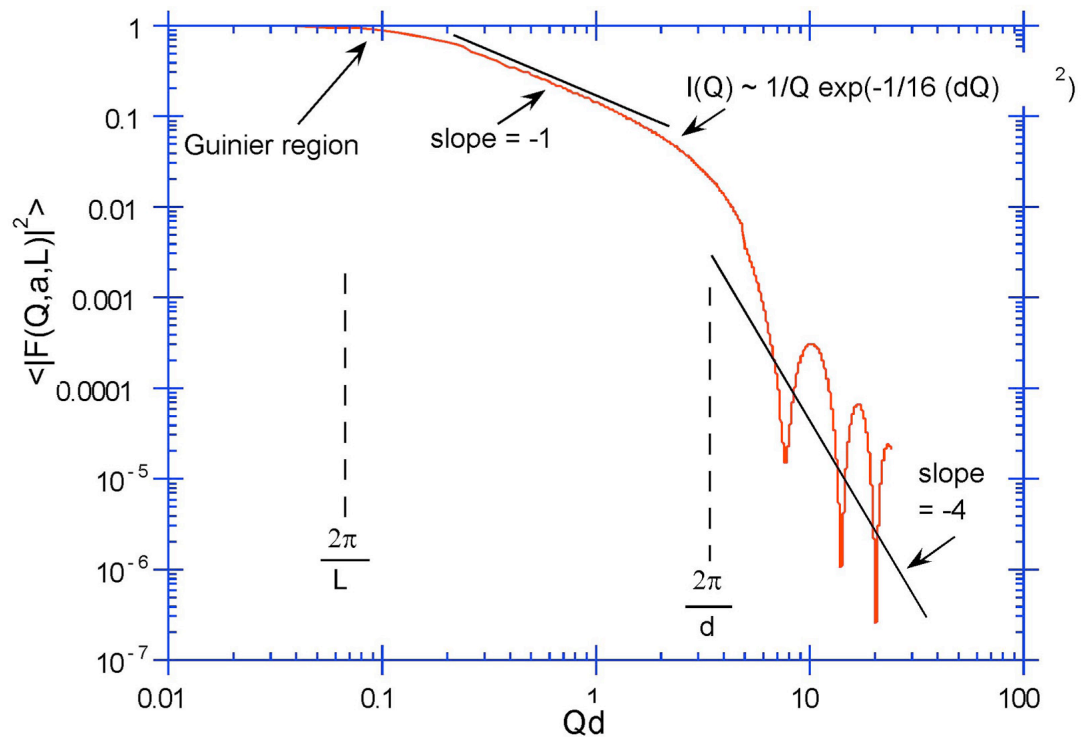
The particle scattering,  $P(q)$ , depends on the shape of the particle

$$P(q) = \int \Delta\rho^2 \frac{\sin(qr)}{qr} 4\pi r^2 dr$$

E.g., Form factor,  $F(q)$ , for rods length  $L = 80$  nm, diameter  $d = 4$  nm

Guinier region

$$I(q) = P(0) \exp\left[-\frac{q^2 R_g^2}{3}\right]$$





# Small-angle X-ray Scattering

The Structure Factor,  $S(q)$ , given by relative arrangement of particles

$S(q)$  is related to statistical descriptions of the particle positions:

the particle-particle pair correlation functions,  $g(r)$

Computationally convenient.  $S(q)$  can be calculated just like the Debye Eqn for x-ray diffraction

e.g., for  $N$  particles of known position

$$S(q) = 1 + \frac{1}{N} \sum_{i=1}^{N-1} \sum_{j=i+1}^N \frac{\sin(qr_{ij})}{qr_{ij}}$$

... this is a discrete sin-transform of  $g(r)$ !



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# Small-angle X-ray Scattering

The Structure Factor,  $S(q)$ , given by FT of the pair correlation function,  $g(r)$

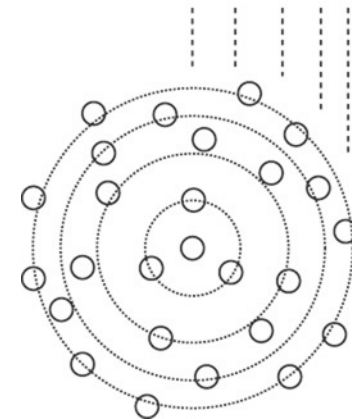
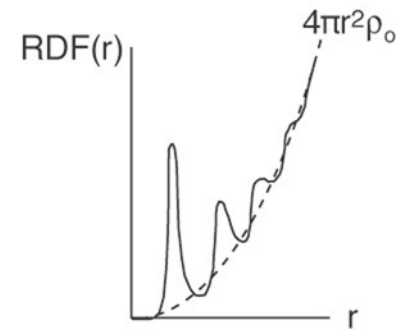
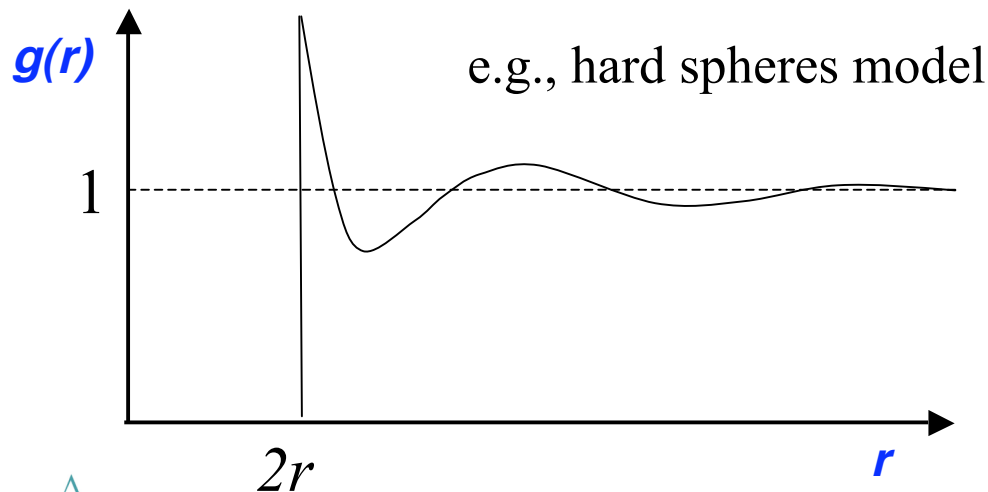
$$S(q) = 1 + \frac{N}{V} \int 4\pi r^2 [g(r) - 1] \frac{\sin(qr)}{qr} dr$$

## Definition of $g(r)$

1D representation of 3D structure

Related to the **radial distribution function** (RDF)

Probability of finding another particle within  $r \rightarrow r + \delta r$



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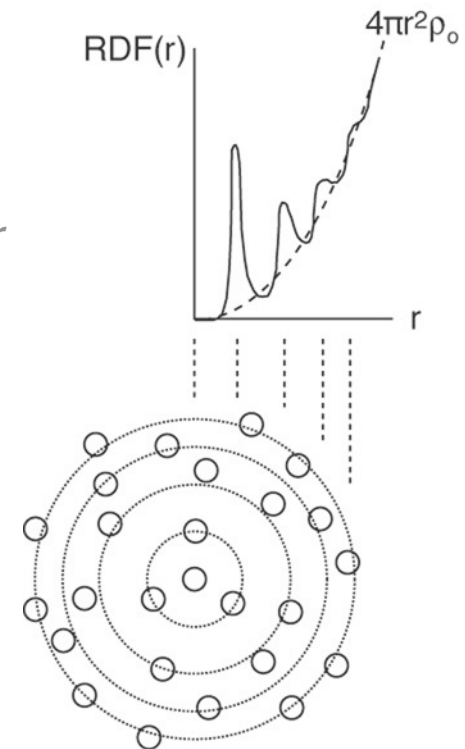
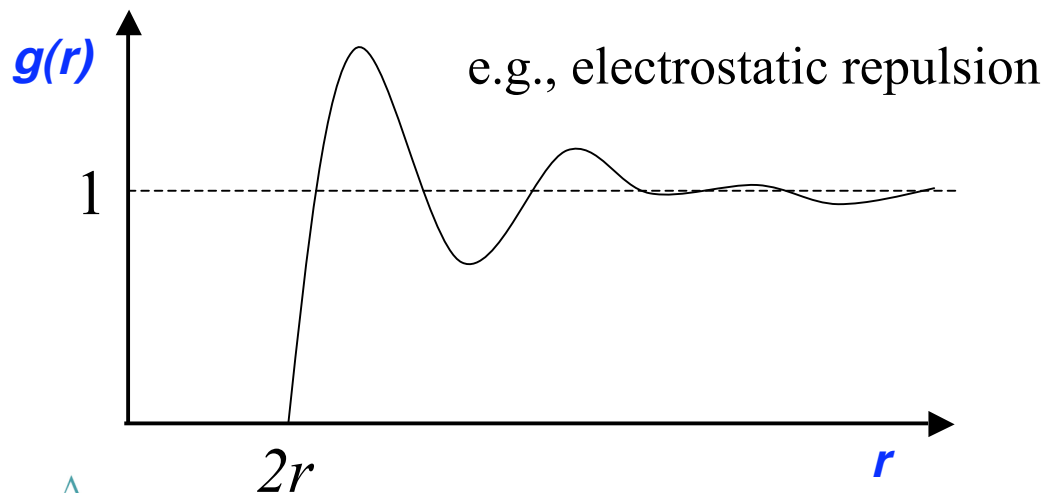
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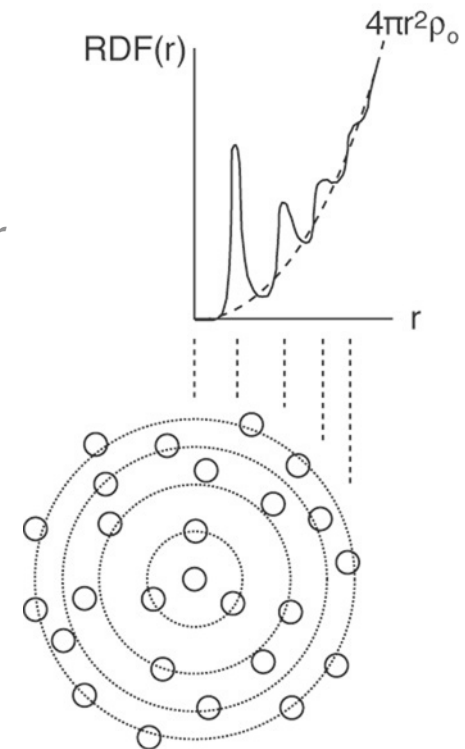
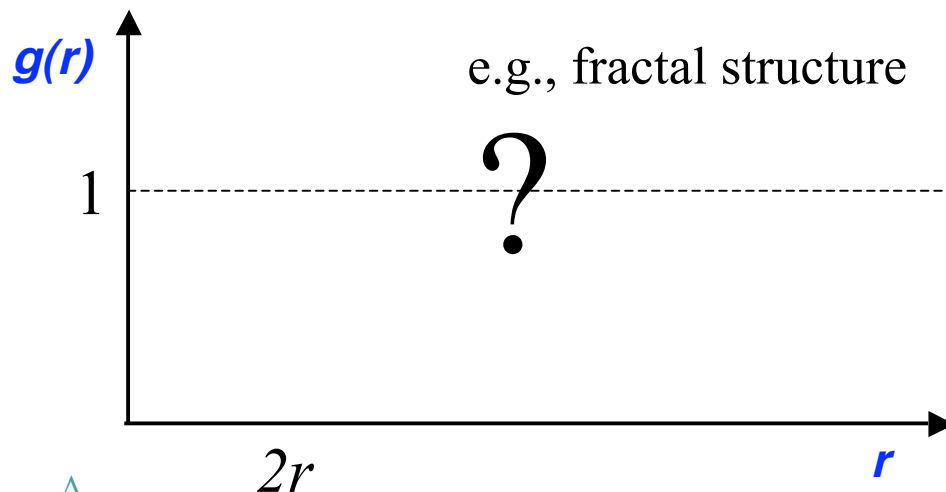
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# Small-angle X-ray Scattering

Analysis of SAXS data for aggregates = **estimating  $g(r)$**

## I. Analytical expression for $g(r)$

e.g. fractal aggregates

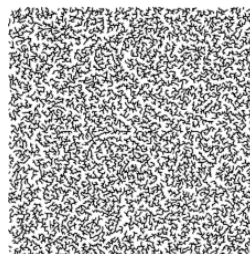
$$[g(r) - 1] \propto r^{D_F - 3} \exp(-r/\xi)$$

e.g. hard spheres

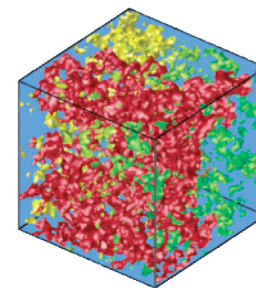
Complex coupled equations

## II. Simulate $g(r)$

constrain  $n(r)$ ,  $P(q)$



van Garderen et al.,  
*J. Chem. Phys.* **102**,  
480 (1995)



*Computer  
model*

Hedstrom et al.,  
*Langmuir* **20**, 1535 (2004)

*Simulated SAXS*



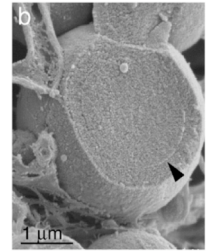
*Experimental SAXS*



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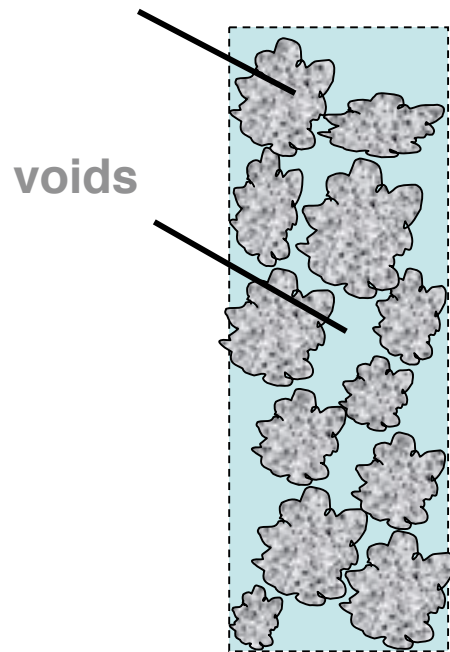
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# SAXS from Porous Media

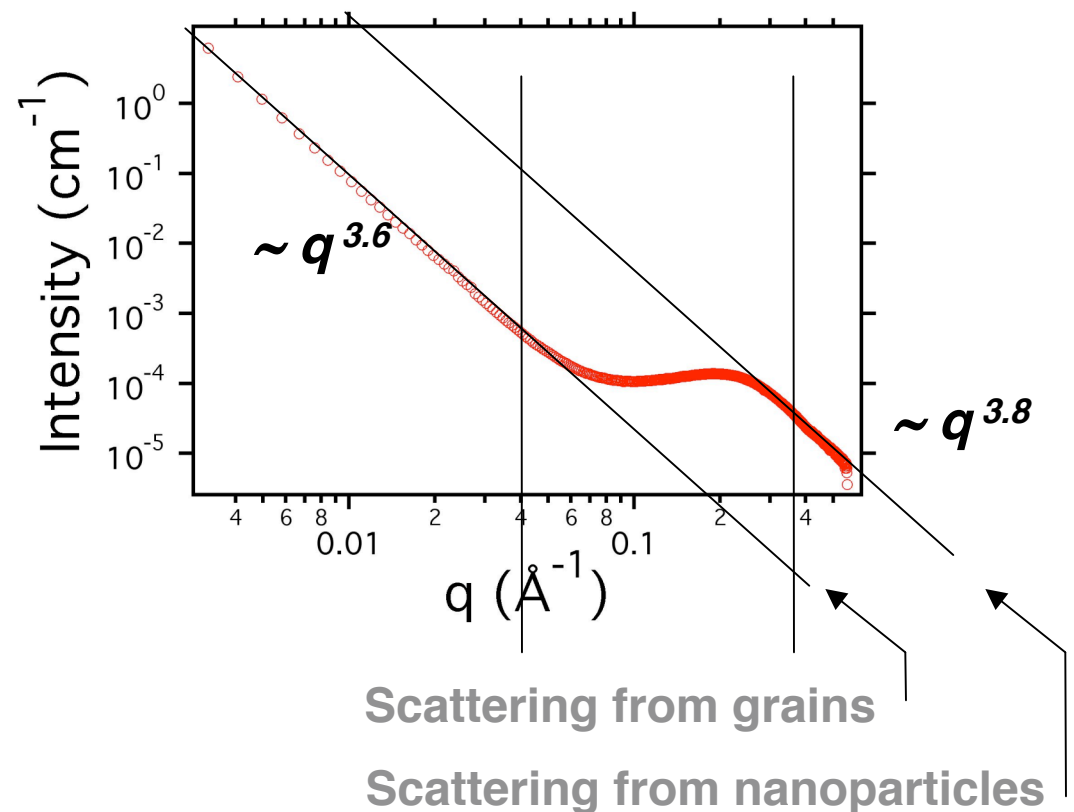


Two length scales - *two Porod regions*

porous grains



SAXS from dried ZnS nanoparticles



Theory: Spalla et al., *J. Appl. Cryst.* **36**, 338 (2003)

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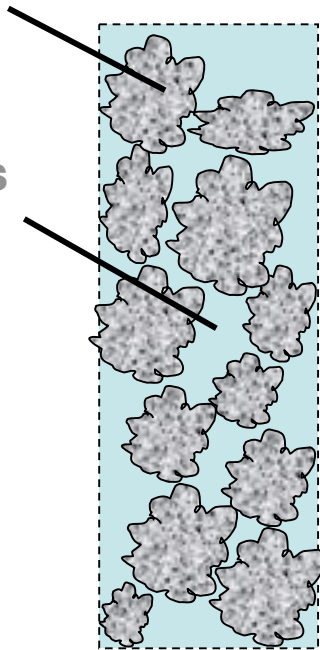
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# SAXS from Porous Media

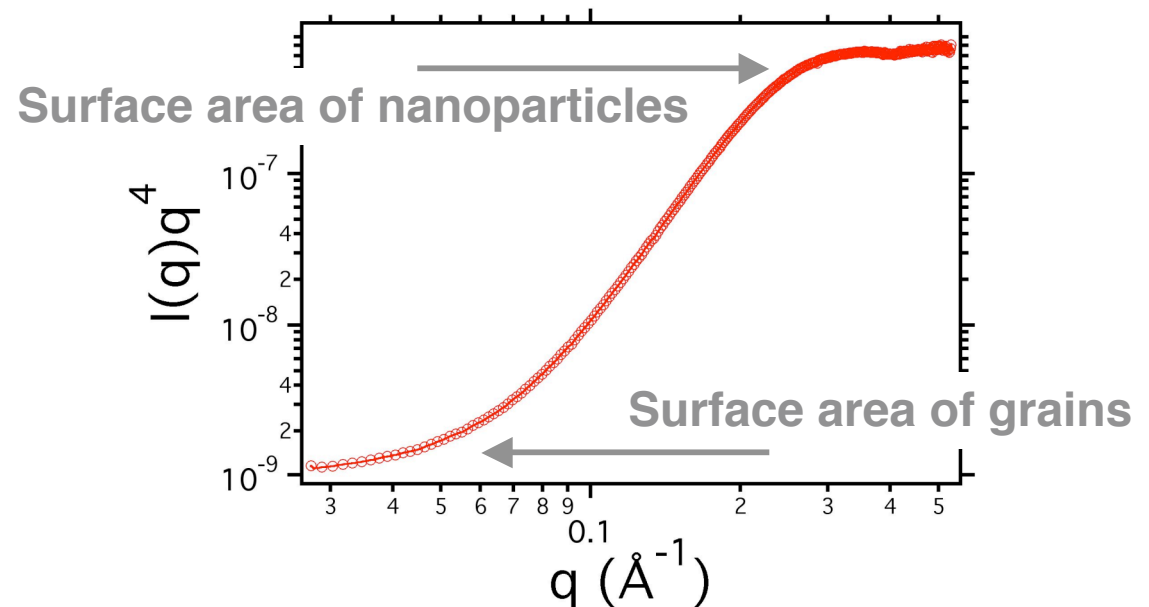
Two length scales - *two Porod regions*

porous grains

voids



Asymptotes give two surface areas



Ratio of surface areas = 600



Theory: Spalla et al., *J. Appl. Cryst.* **36**, 338 (2003)

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# Colloid Behavior of Goethite Nanoparticles

Research plan:

**SAXS of nanoparticle dispersions**

interparticle interaction forces

**Simulations of aggregation**

real-space aggregate structure

**SAXS of aggregates**

test simulations

**Calculation of hydrodynamic properties**

**Larger scale transport experiments**



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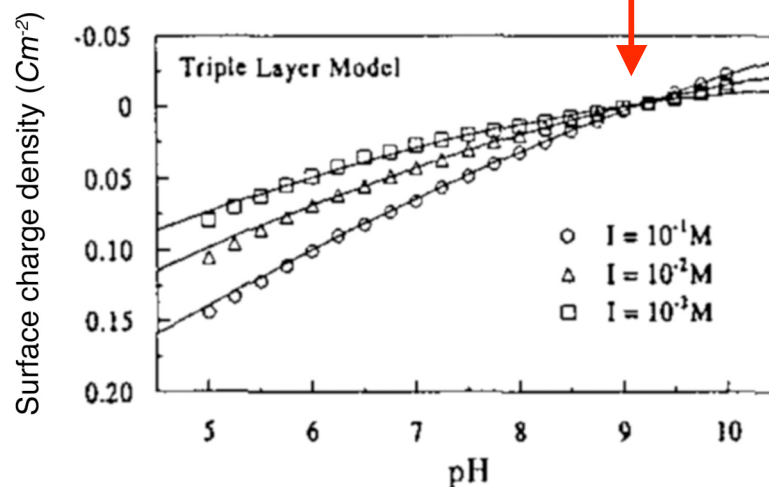
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# Colloid Behavior of Goethite Nanoparticles

Surface charge vs. pH

$\text{pH}_{\text{ZPC}} \approx 9.1$



Lumsdon & Evans, *J. Coll. Interf. Sci.*  
**164**, 119 (1993)



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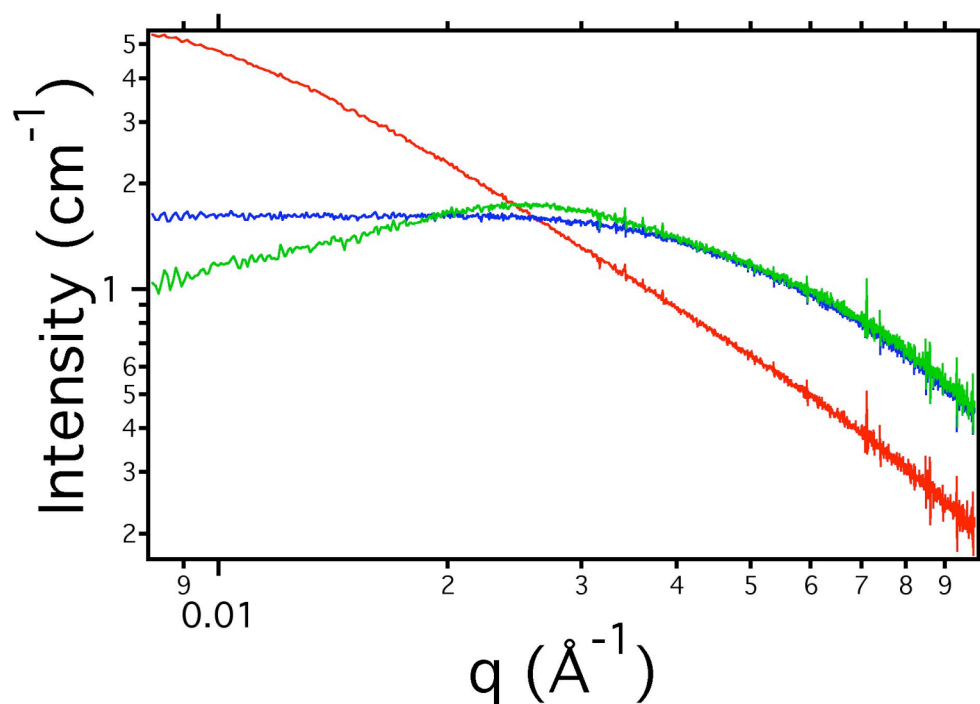
# Colloid Behavior of Goethite Nanoparticles

SAXS of 6 nm diameter FeOOH nanoparticles at pH 5.0 vs. ionic strength

$10^{-2} \text{ M NaNO}_3$

$10^{-3} \text{ M NaNO}_3$

$10^{-4} \text{ M NaNO}_3$



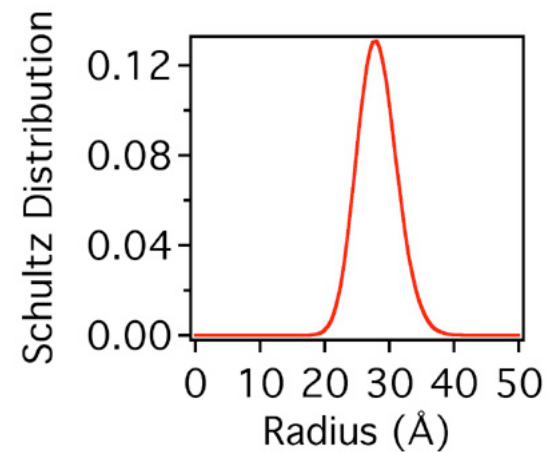
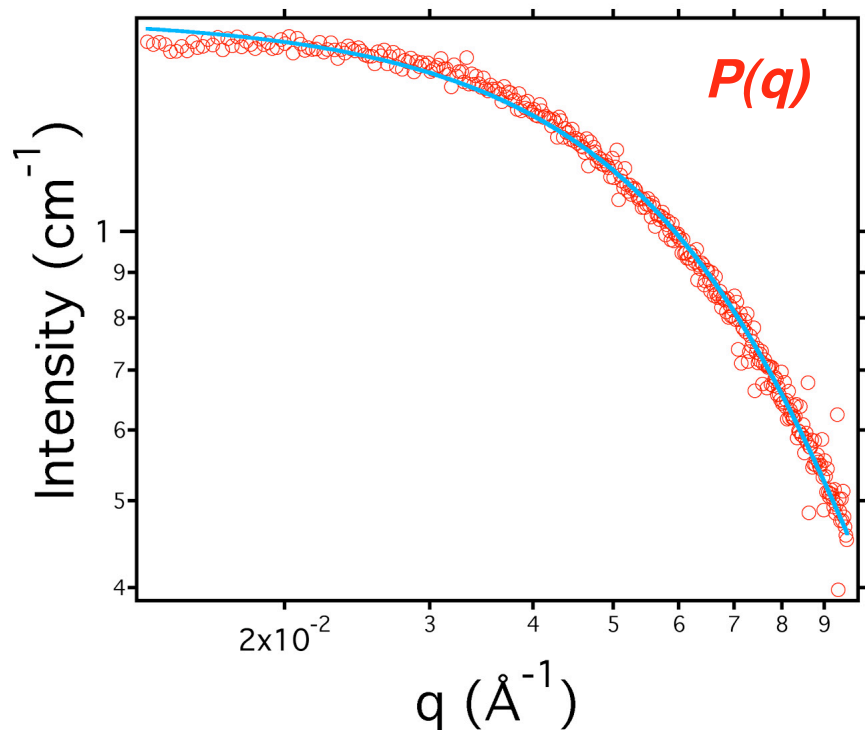
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# Colloid Behavior of Goethite Nanoparticles

Single particle scattering at pH 5.0 and  $10^{-3}$  M  $\text{NaNO}_3$

Fit particle size and size distribution



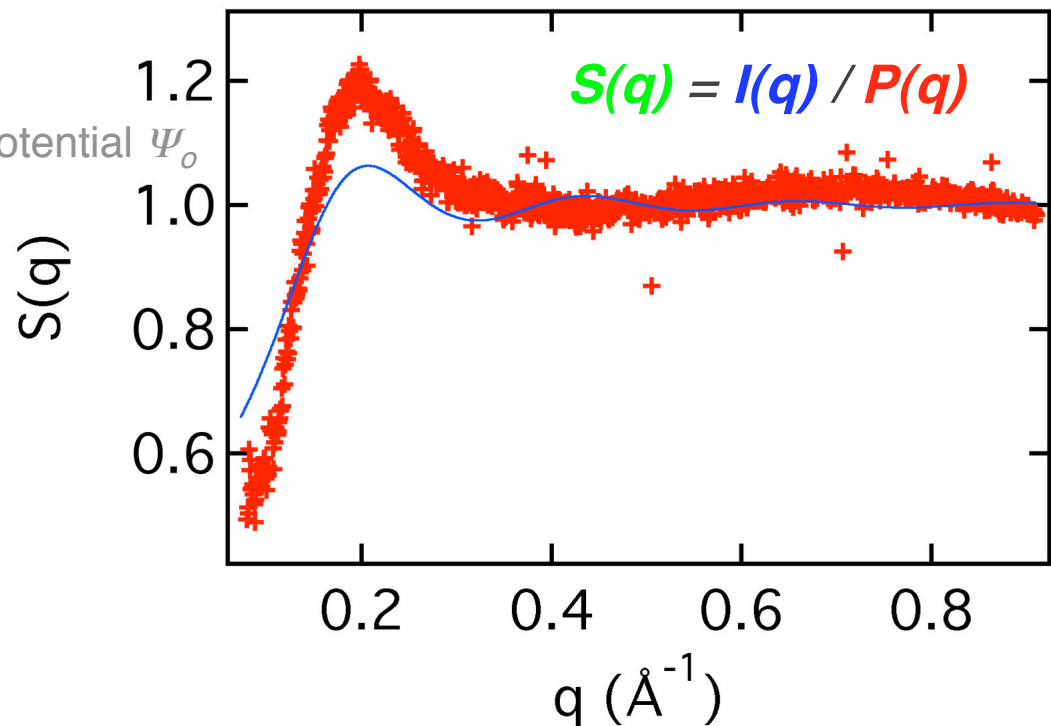
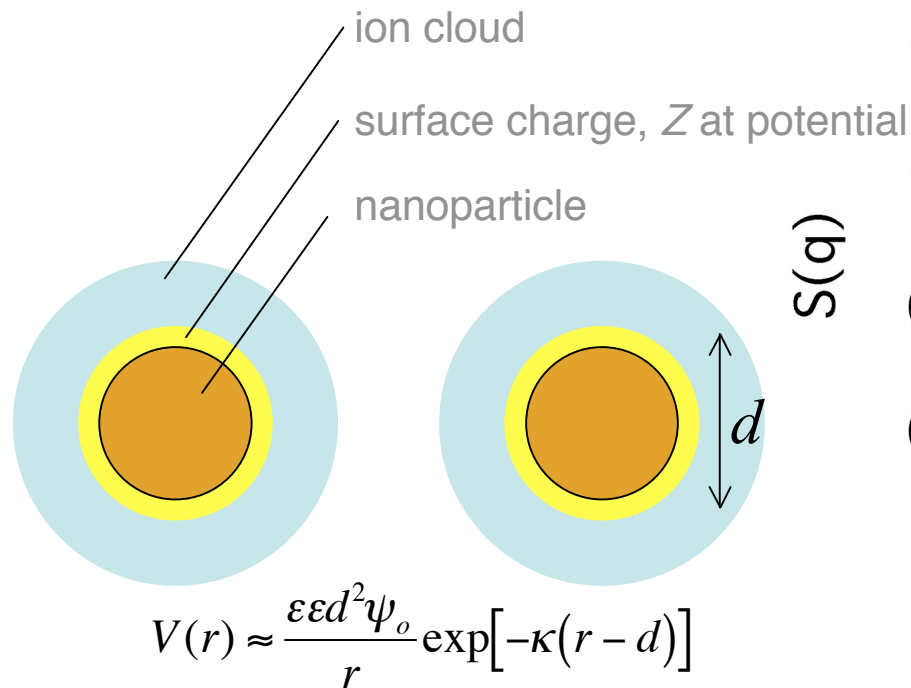
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# Colloid Behavior of Goethite Nanoparticles

Structure factor at **pH 5.0** and  **$10^{-4}$  M  $\text{NaNO}_3$**

Fit electrostatic parameters,  $Z^{\text{eff}}$ ,  $\kappa^{\text{eff}}$ .



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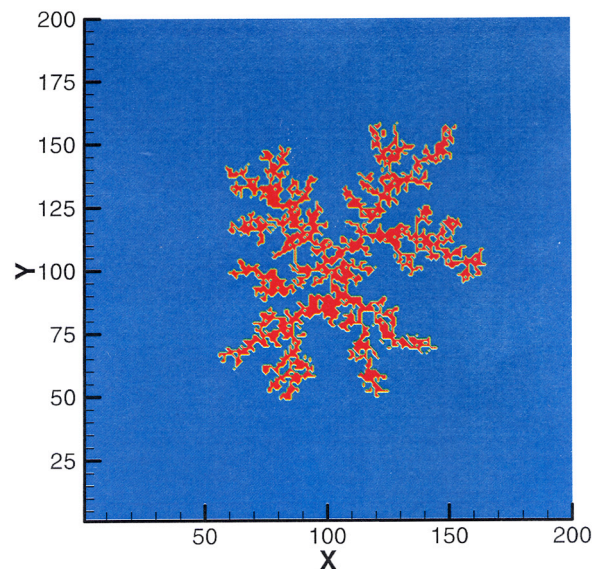
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# Simulating the Structure of Goethite Nanoparticle Aggregates

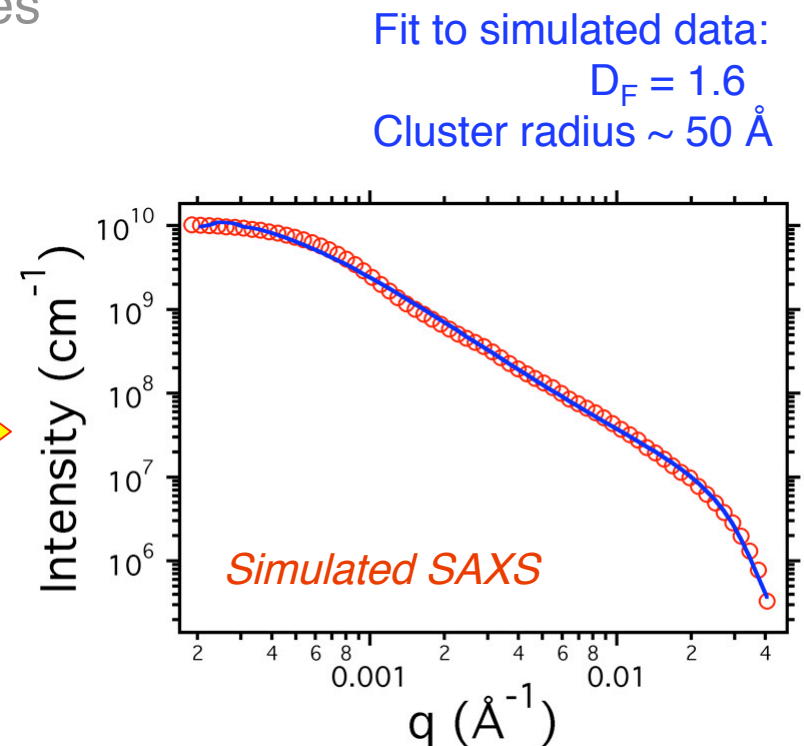
## Lattice Boltzmann:

Currently limited to 2D!

growth of fractal crystal structures  
simulated SAXS patterns



LB Simulation by Guopeng Lu



**LB Theory:** Kang et al., *Geophys. Res. Lett.* **31**, L21604 (2004)

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# SAXS from Fractal Aggregates

## Two length scales

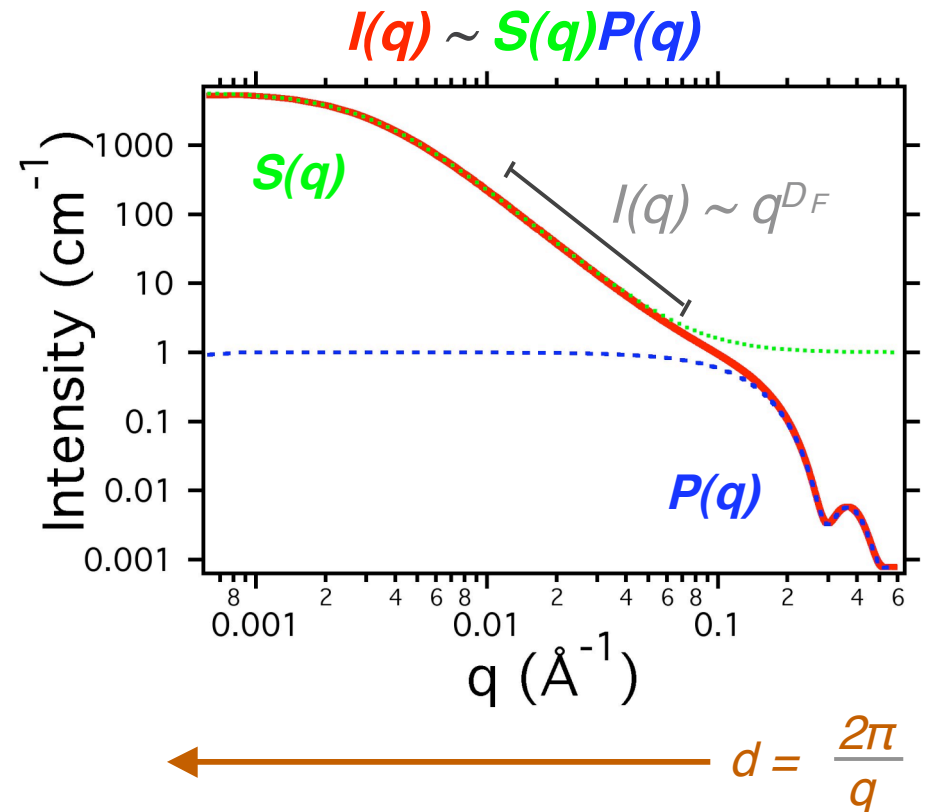
individual particle size,  $r_o$   
largest cluster size,  $\xi$

$$[g(r) - 1] \propto \frac{r^{D_F - 3}}{r_o^{D_F}} \exp(-r/\xi)$$

## Fractal dimension, $D_F$

Efficiency of space filling

## SAXS can measure size & $D_F$ ANALYTICAL APPROACH



Teixeira, *J. Appl. Cryst.* **21**, 781 (1988)

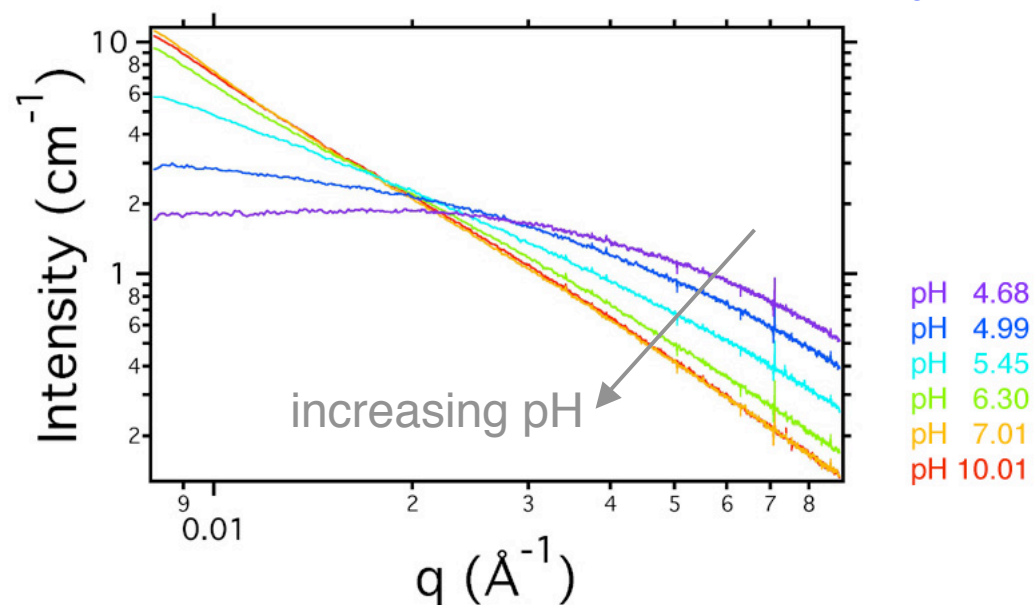


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# Colloid Behavior of Goethite Nanoparticles

SAXS of 6 nm diameter FeOOH nanoparticles vs. pH  
Volume Fraction = 0.075 %;  $10^{-2}$  M NaNO<sub>3</sub>

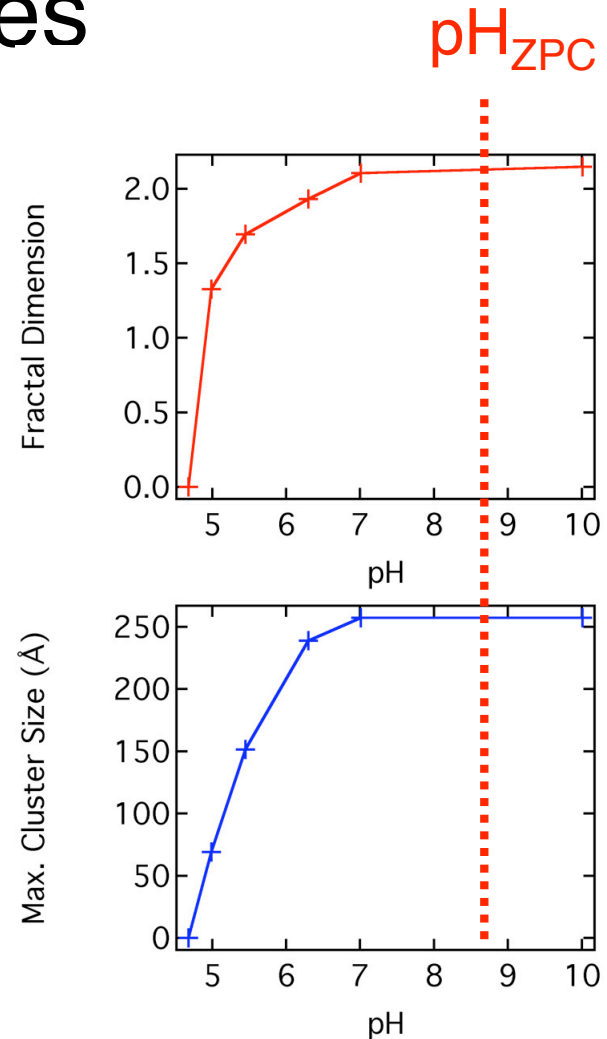
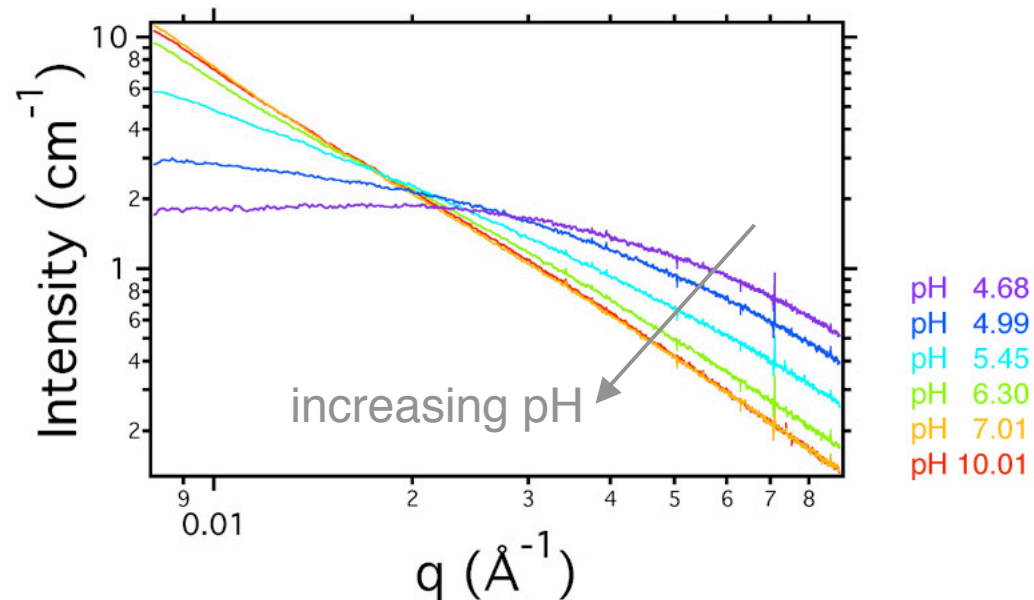


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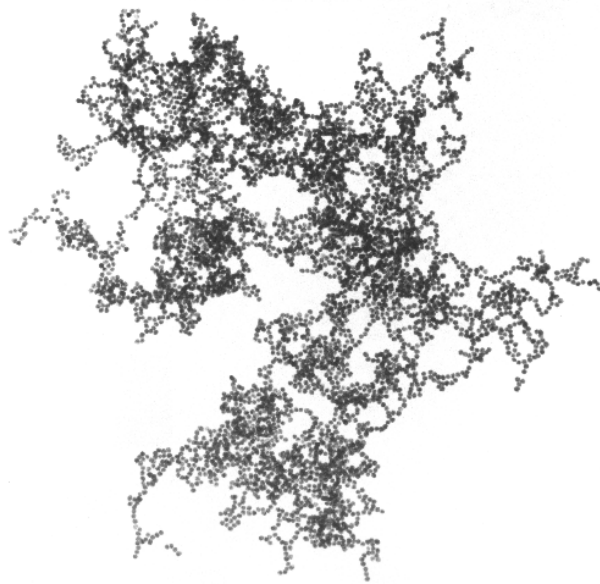
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# SAXS from Fractal Aggregates

## Numerical simulation

Reveals breakdown of fractal description at low  $r$



Fractal properties not well-defined for  $< 50$  particles

Lattuada et al., *J. Coll. Interf. Sci.* **268**, 106 (2003)

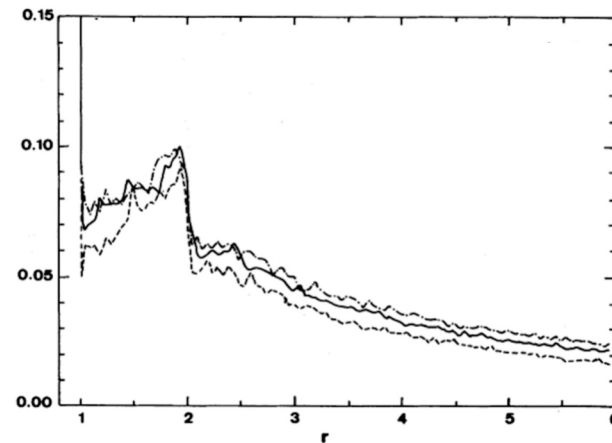


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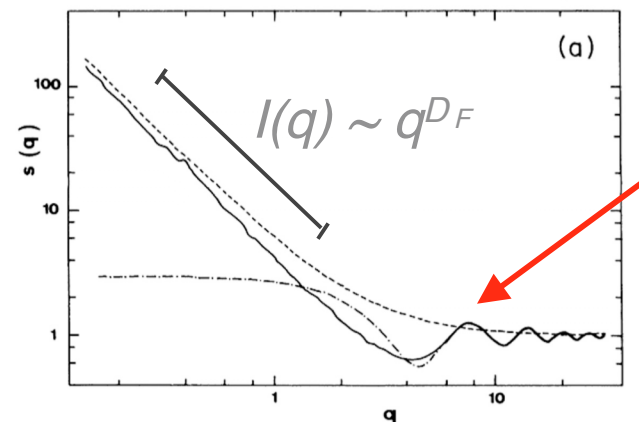
## Monodisperse particles

Sharp peaks in  $g(r)$  and  $S(q)$

$g(r)$



$S(q)$



Hasmy et al., *Phys. Rev. B* **48**, 9345 (1993)

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# Conclusions

- Coulombic repulsion evident in non-aggregated suspensions of goethite nanoparticles.
  - Larger data set and better analysis required to parameterize effective pair potentials
- Nanoparticles form aggregated clusters with fractal internal structure well below the  $\text{pH}_{\text{zpc}}$ 
  - Morphology & short-range structure uncertain
- Cluster size and density dependent on solution condition, as expected
  - What determines maximum cluster size?

# Simulating the Structure of Goethite Nanoparticle Aggregates

Long term goal:

**Lattice Boltzmann simulations**  
interparticle interaction forces  
hydrodynamic behavior

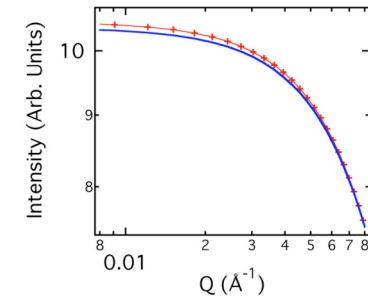
Alternative:

**Simulated annealing**  
no physical description  
seek agreement with SAXS data

# Simulating the Structure of Goethite Nanoparticle Aggregates

Simulated annealing:

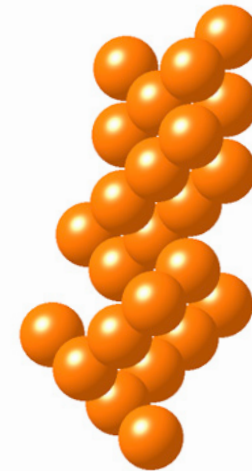
DAMMIN code optimized for macromolecules  
porous structures possible in principle



pH 4.99



pH 5.45



pH 6.30



Svergun, *Biophysical J.* **76**, 2879 (1999)

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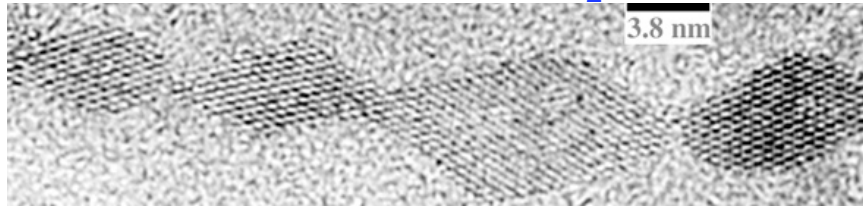
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# Simulating the Structure of Goethite Nanoparticle Aggregates

## Linear aggregates?

TEM observations and MD simulation highlight role of *anisotropic structure*

TiO<sub>2</sub> nanoparticles

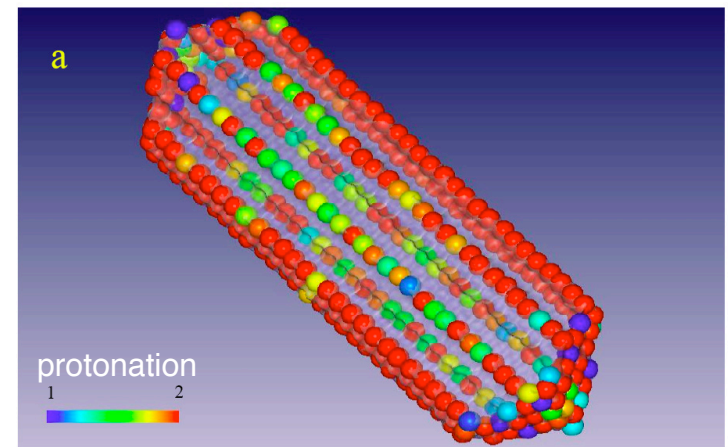
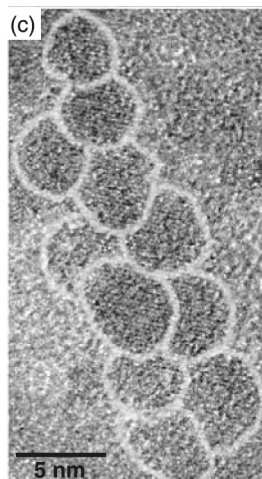


Penn & Banfield *Am. Mineral.* **83**, 1077 (1998)

Rustad & Felmy *Geochim. Cosmochim. Acta*, **69**, 1405 (2005)

FeOOH nanoparticles

Guyodo et al.,  
*Geophys. Res. Lett.* **30**, 1512  
(2003)



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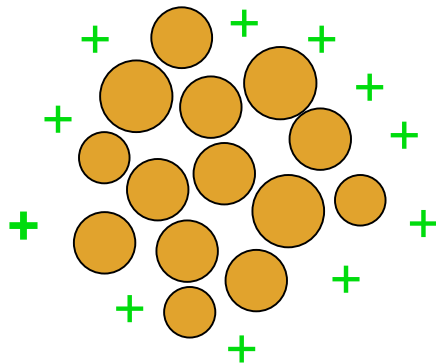
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# Simulating the Structure of Goethite Nanoparticle Aggregates

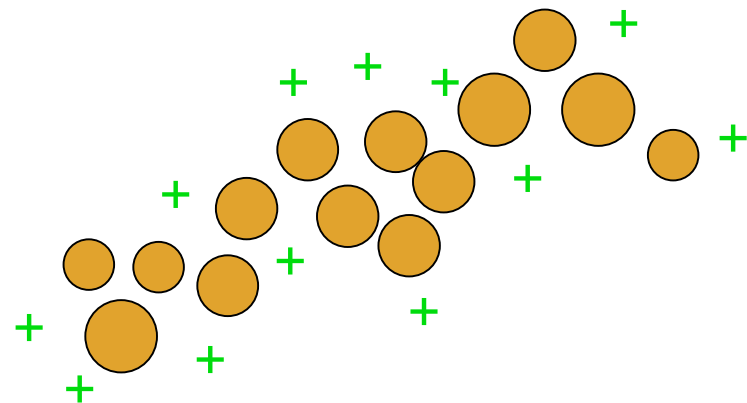
Linear aggregates?

Monte Carlo simulations (2D) highlight role of *repulsive interactions*

High energy aggregate



Low energy aggregate



Lebovka et al., *EuroPhys. Lett.* **41**, 19 (1998)

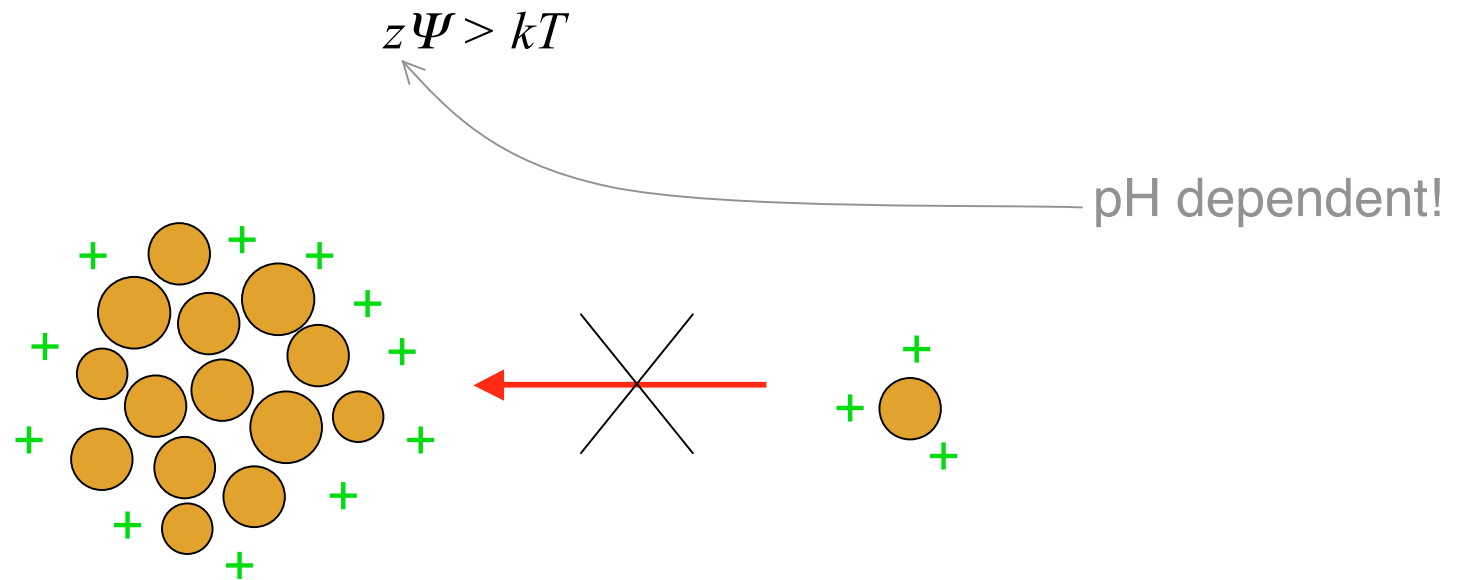
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# Simulating the Structure of Goethite Nanoparticle Aggregates

Repulsive interactions likely limit maximum cluster size

Particle-cluster and cluster-cluster aggregation halts when:



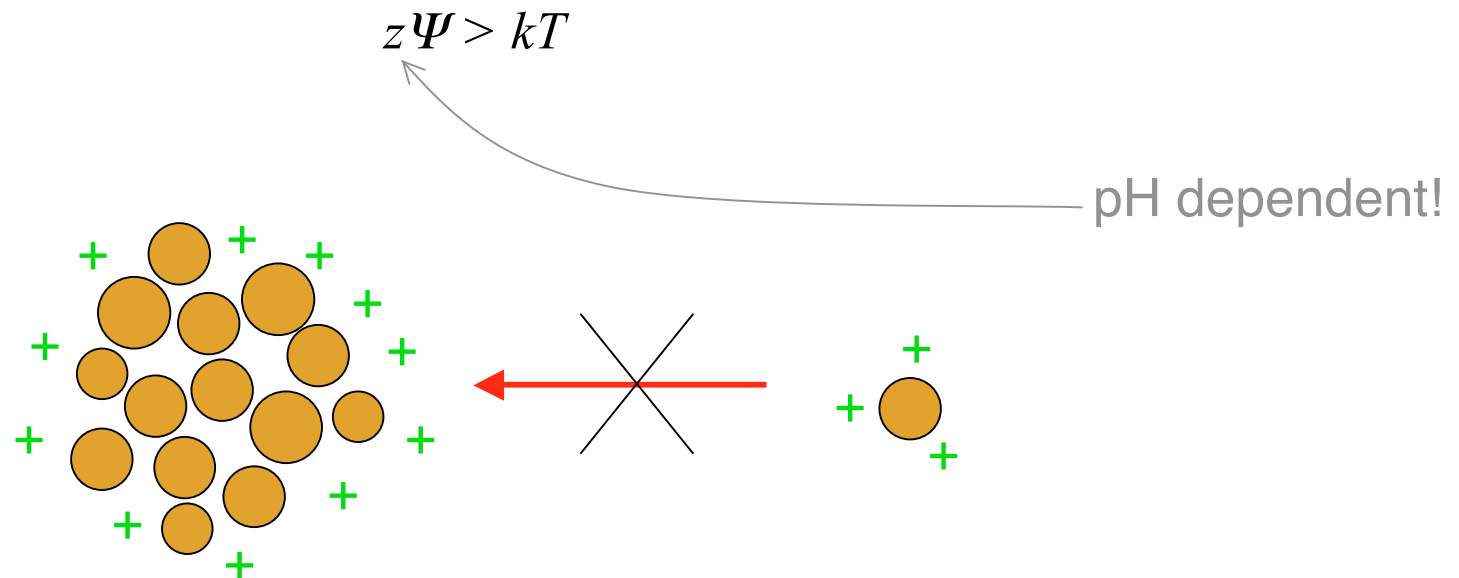
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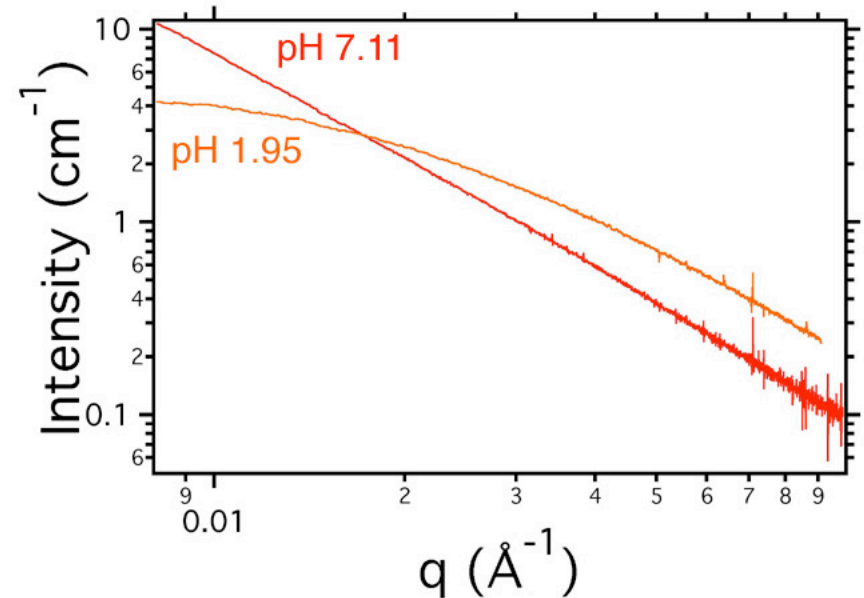
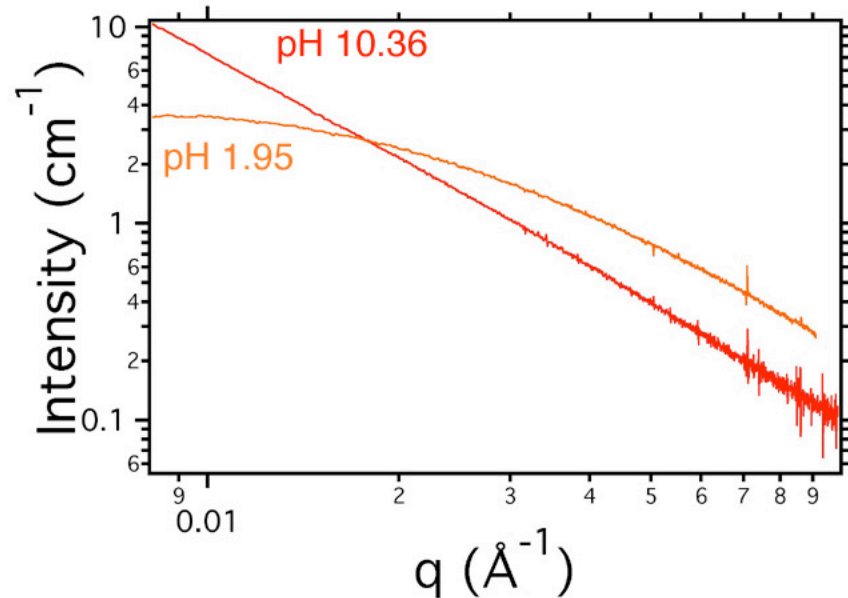
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# Partial Disaggregation of Goethite Clusters

Almost reversible process ...

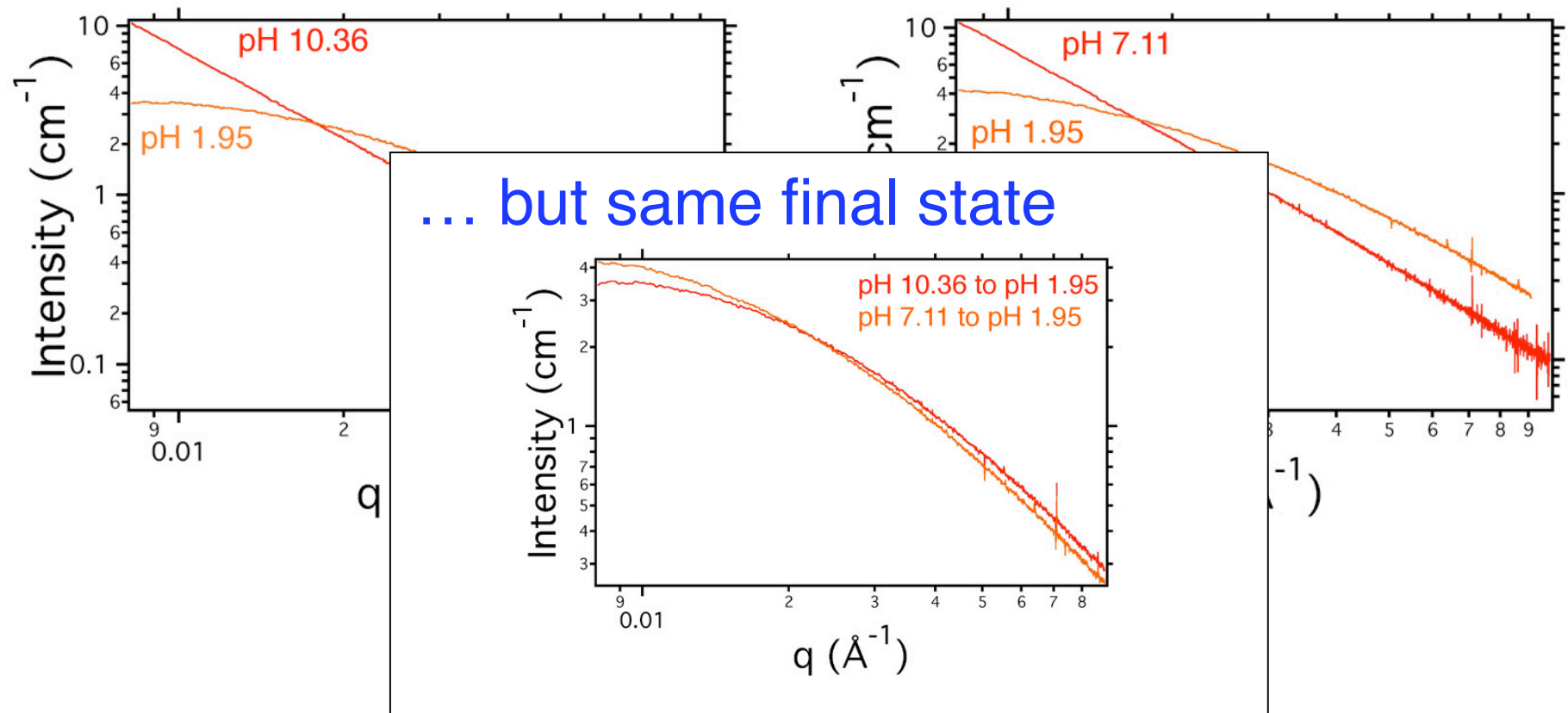


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Almost reversible process ...

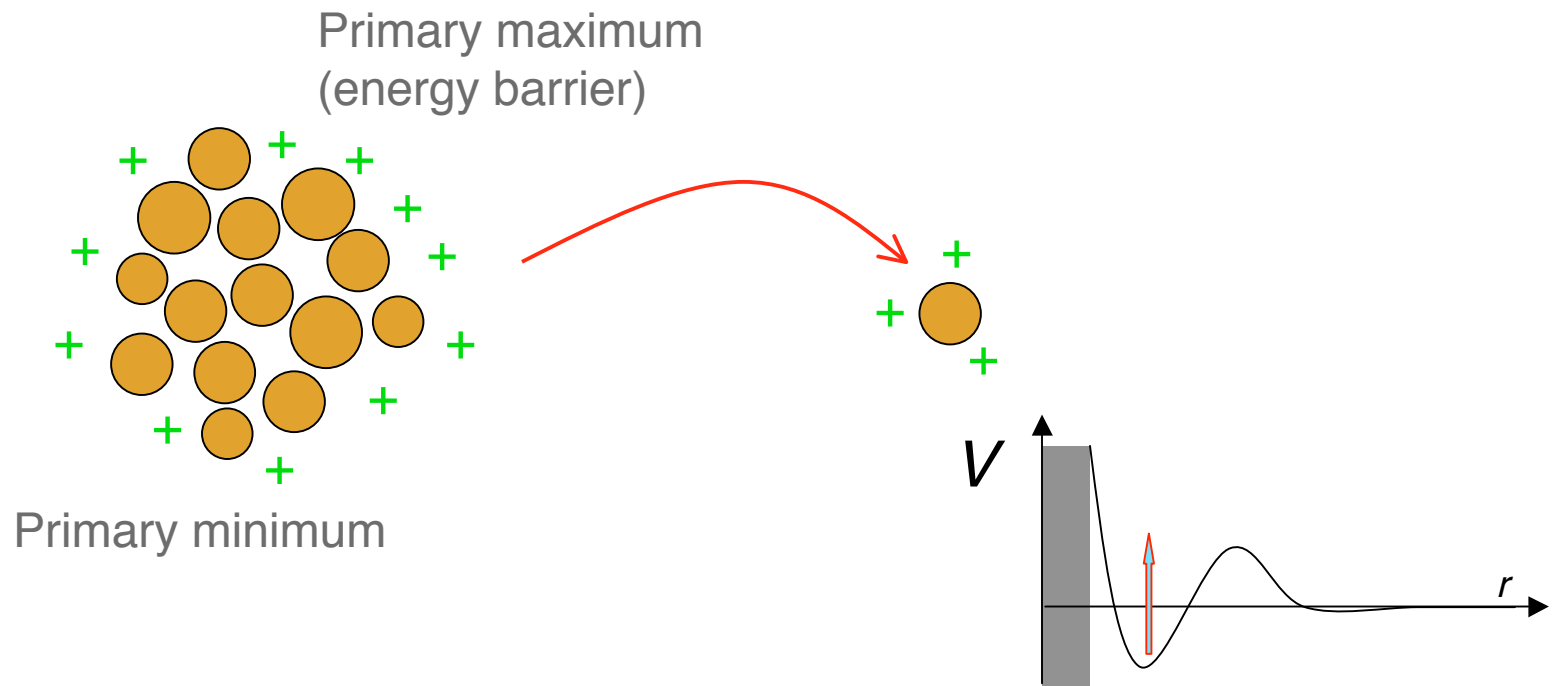


# Partial Disaggregation of Goethite Clusters

## Surface charge drive partial disaggregation?

Finite potential well upon aggregation

Test short-range interaction potentials in simulation



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